

# Memory hierarchy in scheduling simulation: problems, implementation & return of experience

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# Context

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- **Real-time embedded systems (RTES)**

- **Real-time:** must process information and produce responses within a specified time, else risk severe consequences, including failure
  - **Predictability:** compute system temporal timing behaviors at **design time**
  - **Real-time scheduling analysis:** verify the feasibility/schedulability of a system: **feasibility tests**, **scheduling simulation**
- **Challenge:** more and more parallelism and complexity at both software and hardware
  - Even in small systems (drones, cars)
  - Legacy software are no longer executed on specific hardware
  - Less usage of dedicated hardware / more COTS (Federal aviation administration, Commercial Off The Shelf Avionics Software Study, 2011)
    - **Multicore architecture with memory hierarchy**

# Context

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- **Memory hierarchy problem in RTES**

- **Improve the overall system performance, but leads to execution time variability due to **interference** (Lugo et al., 2022)**
  - Cache memory ← Addressed in this talk
  - Memory bus
  - Main memory

- **Verification by scheduling simulation**

- **A common practice of actors in the real-time community**
  - Integration of Cheddar in AADL Inspector
- **Need of support for multi-core**
  - Usage of Cheddar in the Project PLATO (Plasson et al., 2022)

# Problem Statement

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- **Lack of scheduling simulator with support for interference-aware scheduling simulation**

- RTSim (Manacero et al., 2001)
- MAST (Harbour et al., 2001)
- ARTISST (Decotigny et al., 2002)
- STORM (Urunuela et al., 2010)
- YARTISS (Chandarli et al., 2012)
- SimSo (Cheramy et al., 2015)
- Cheddar (Singhoff et al., 2004)

Simulation  
without  
interference

Simulation with  
interference

- **Lack of theoretical research to guarantee the applicability of scheduling simulation as a schedulability test**

# Outline

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## 1. Introduction

## 2. Scheduling simulation with interference

## 3. CRPD-aware scheduling simulation

- **Related work**

- **Background**

- CRPD computation models:  $\mathcal{C}^{off}$  and  $\mathcal{C}^{on}$
- Sustainability analysis

- **CRPD-aware scheduling simulation**

- $\mathcal{C}^{on-lim}$ : an improved CRPD computation model
- Sustainability analysis of  $\mathcal{C}^{on-lim}$
- Feasibility interval of  $\mathcal{C}^{on-lim}$

- **Evaluation**

## 4. Conclusion

# Scheduling simulation with interference

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- **Why scheduling simulation ?**

- **Advantages**

- **Observed reduced pessimism** compared to static WCRT analysis
  - Used as a **sufficient condition** to compare interference-aware WCRT analysis
- **Adaptability/Flexibility** - manageable integration of additional scheduling parameters
- **Observability** - record and analyze properties such as numbers of preemptions and various scheduling events that are not observable by static analysis
- **Analysis** - understand why a system is not schedulable → required by stakeholders

# Scheduling simulation with interference

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- **Why scheduling simulation ?**

- **Limitations**

- **Scalability** - especially when mixing timing specifications of different orders of magnitude; e.g: WCET and cache block reload time.
- **Analysis** - tons of trace, e.g: level of abstraction (timing, system type) during simulation
- **Engineering challenges** - how to implement the simulator
- **2 theoretical problems: sustainability and feasibility interval** (to be detailed later)

# Scheduling simulation with interference

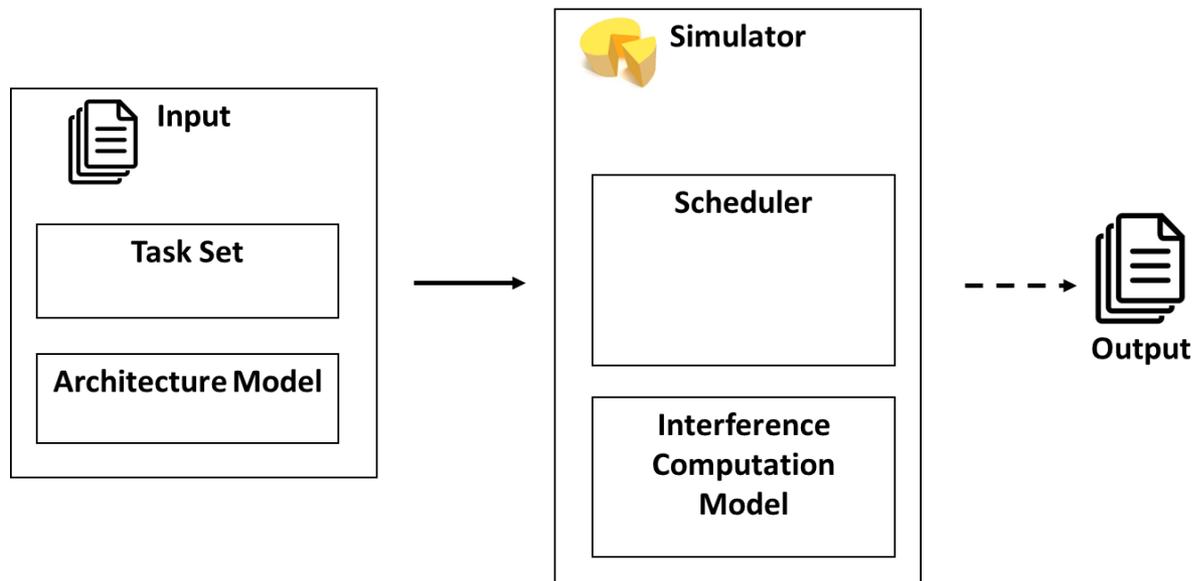
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- **Scheduling simulation**

- Simulation of a **task set**  $T$  on an **architecture**  $M$  under a **scheduler**  $S$  over an **interval of time**  $F$

- **Interference-aware scheduling simulation**

- **Scheduling simulation with an interference computation model**  $I$ 
  - Describe the method of computing the interference added to the execution time of a task during its execution



# Scheduling simulation with interference

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- **We investigated cache memory interference for uniprocessor with one level of direct-mapped instruction cache**
  - **A tiny portion of the interference-aware scheduling simulation problem !**
- **... and we found the following problems**
  - **Problem 1: How to model and compute the interference**
    - What should we consider to simulate the worst-cases
    - Pessimistic of the computation model
  - **Problem 2: Sustainability problem**
    - If a system is considered to be schedulable by simulation with the worst-case parameter, is it schedulable in better cases ?
  - **Problem 3: Feasibility interval problem**
    - How long should we simulate ?
  - **Problem 4: Simulator performance**
    - Mixing timing specifications of different orders of magnitude = (very) long simulation period

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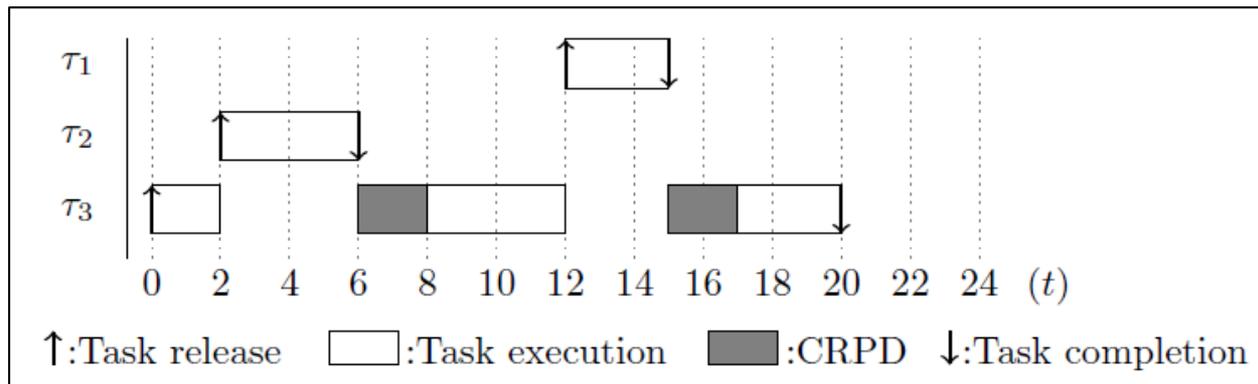
## 4. Conclusion

# Problem Statement

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- **Cache memory in RTES**

- **Cache related preemption delay (CRPD):** the additional time to refill the cache with memory blocks evicted by preemptions



- CRPD is a non-negligible preemption cost, can present up to 44% of the WCET (Pellizzoni et al., 2007)
- Create scheduling anomalies and complex optimization problems (Phavorin et al., 2015) which require extensions of classical scheduling analysis

# Problem Statement

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- **CRPD-aware scheduling simulation**

1. **Pessimistic**: a system requires significantly **more** computing resources to be schedulable
2. **Non sustainable**: a system is **schedulable under its worst-case** specification but **not schedulable in better cases** when interference is present
3. **Unidentified feasibility interval**: how long should we run the simulation ?

The three problems limit the applicability and the usage of scheduling simulation as a verification methods for RTES with memory hierarchy

# Related Work

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- **CRPD-aware scheduling analysis**

- **Analytical-based approaches**

- **CRPD-aware worst-case response time analysis**: Lee et al., 1998; Busquets-Mataix et al., 1996, Tomiyama et al., 2000; Staschulat et al., 2005; Altmeyer et al., 2012; Lunniss et al., 2014
- **Eliminate or limit the effect of CRPD**: Bertogna et al., 2011; Luniss et al., 2012; Altmeyer et al., 2015;
- **Optimal scheduling**: Phavorin et al., 2017

- **Scheduling simulation based approaches**

- **Simulators without cache support**

- **MAST** (Harbour et al., 2001),
- **STORM** (Urunuela et al., 2010),
- **YARTISS** (Chandarli et al., 2012)

- **Simulators with cache support**

- **SimSo** (Cheramy et al., 2015): Stack Distance Profile
- **Cheddar** (Tran et al., 2014): Useful Cache Block/Evicting Cache Block

# Background

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- **CRPD-aware scheduling simulation**

- **Scheduling simulation with a CRPD computation model  $C$** 
  - Describe the method of computing the CRPD added to the execution time of a task when it resumes **after a preemption**

- **System model and assumptions**

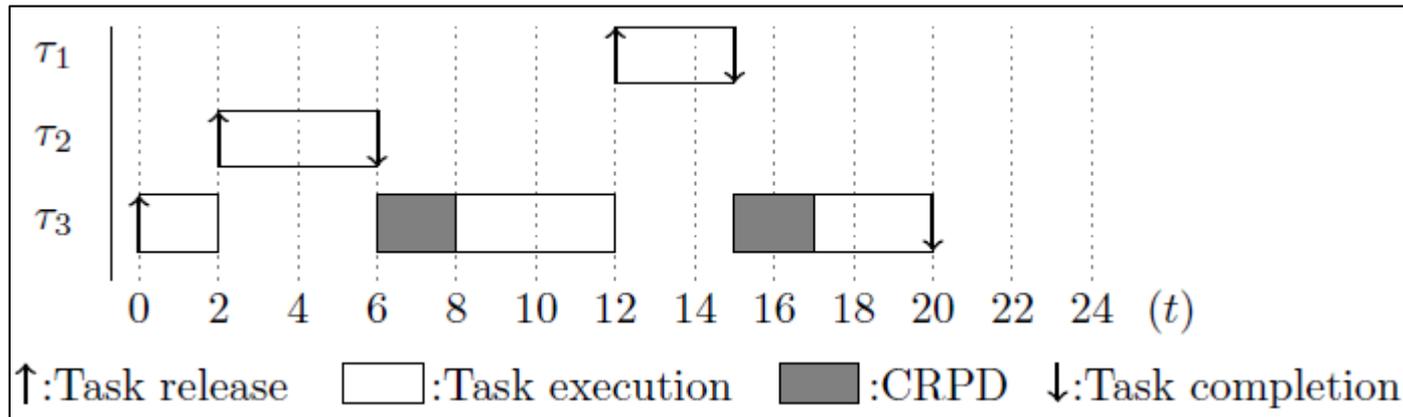
- **$T$ : a set of periodic tasks  $\tau_i(C_i, T_i, D_i, \Pi_i, O_i)$  - capacity, period, deadline, priority and offset**
- **$M$ : uniprocessor with one level of direct mapped instruction cache**
- **$S$ : fixed priority preemptive scheduling**
- **$C$ :  $C^{off}$ ,  $C^{on}$ ,  $C^{on-lim}$**
- **$F$ : to be defined**

# Background

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- $C^{off}$ : offline CRPD computation model

- The CRPD when a task  $\tau_i$  is preempted is **fixed** and **computed offline**
  - CRPD  $\gamma_i$  is added to the remaining capacity of  $\tau_i$  whenever the task is preempted



- **Pessimistic because the preempting tasks may not evict the data in the cache of the preempted task**
  - The pessimism also depends on the method of computing the CRPD offline

# Background

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- **$C^{on}$ : online CRPD computation model**

- For task  $\tau_i$  a set of useful cache blocks ( $UCB_i$ ) and evicting cache blocks ( $ECB_i$ ) are computed before simulation
  - $UCB_i$  (Lee et al., 1998): cache blocks used by a task that are reused later on and will have to be reloaded if evicted from the cache due to preemption
  - $ECB_i$  (Busquets-Mataix et al., 1996): cache blocks used by a task that may override some cache locations used by the preempted task

- **CRPD computation**

- $UCB_i^t$ : the set of UCB of  $\tau_i$  in the cache at time  $t$
- $\tau_i$  is preempted by  $\tau_j$  at time  $t$

$$UCB_i^t = UCB_i^{t-1} - (UCB_i^{t-1} \cap ECB_j)$$

- $\tau_i$  resumes execution at time  $t+\Delta$

$$\gamma_i^{t+\Delta} = |UCB_i - UCB_i^{t+\Delta}| \cdot BRT$$

# Background

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- **Sustainability analysis**

- Definition (Goossens et al., 1997): a given scheduling policy and/or a schedulability test is sustainable if any system that is schedulable under its **worst-case** specification remains so when its behavior is **better** than the worst-case
- The term "**better**" means that the parameters of one or more individual task(s) are changed in any, some, or all of the following ways
  - (1) **reduced capacity**
  - (2) **larger period**
  - (3) **larger relative deadline**

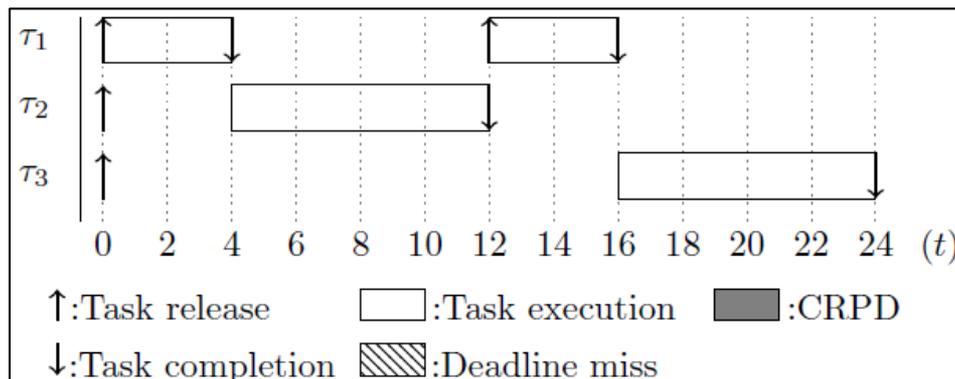
# Background

- Sustainability of  $C^{on}$

- Example 1

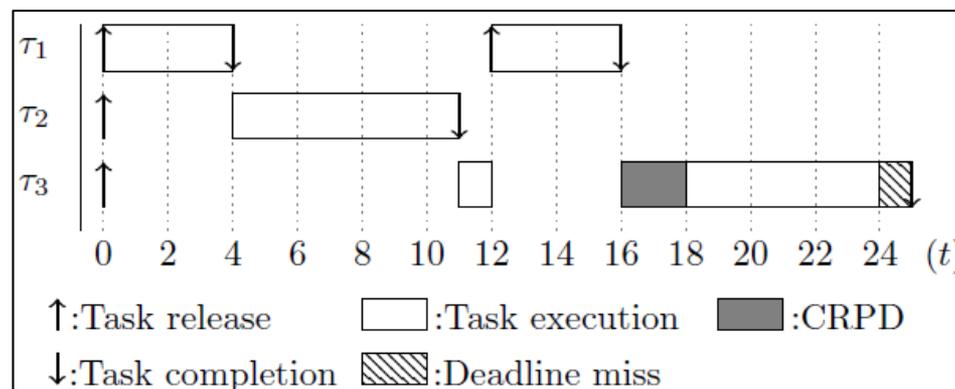
Task	$C_i$	$T_i$	$D_i$	$O_i$	$\Pi_i$	UCB <sub>i</sub>	ECB <sub>i</sub>
$\tau_1$	4	12	12	0	3	$\emptyset$	{1,2}
$\tau_2$	8	24	24	0	2	{3}	{3,4}
$\tau_3$	8	24	24	0	1	{1,2}	{1,2}

- Case 1: original task set



- Case 2: reduced capacity of  $\tau_2$

- $C'_2 = 7 (< C_2 = 8)$
    - $\tau_3$  missed its deadline
    - **Non sustainable scheduling with regard to the capacity parameter**



# Approach

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- **$C^{on-lim}$** : an improved online CRPD computation model
  - The CRPD is at most be proportional to the executed capacity (Luniss, 2014)
    - The CRPD is related to the amount of useful information that has to be reloaded into the cache
    - If a task is preempted shortly after it starts, it has not yet loaded all of the UCBs and will therefore not experience the maximum CRPD
- **CRPD computation**
  - Notation:  $\rho_i^t$  - number of UCBs **loaded** into the cache at time  $t$
  - The number of UCBs in the cache at time  $t + \Delta$ 
$$\rho_i^{t+\Delta} = \min(|UCB_i|, \rho_i^t + \lfloor \frac{\Delta}{BRT} \rfloor)$$
  - CRPD computation when  $\tau_i$  resumes at time  $t$ 
$$\gamma_i^t = \min(|UCB_i - UCB_i^t|, \rho_i^t) \cdot BRT$$

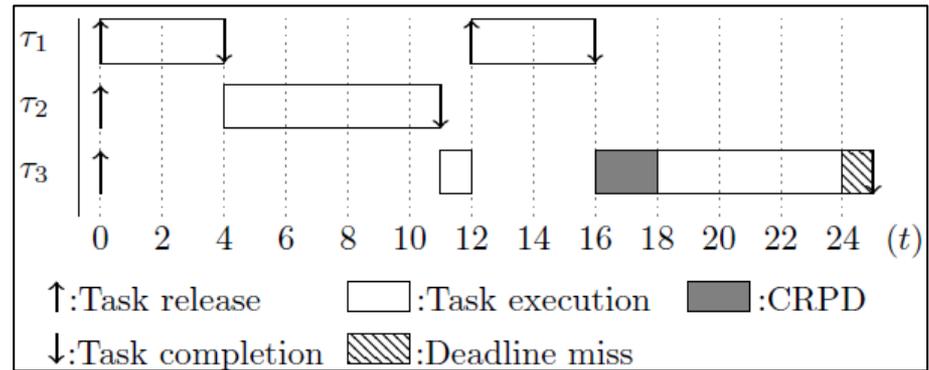
# Approach

- $C^{on-lim}$ : an improved online CRPD computation model

- Example 1 case 2

with  $C^{on}$

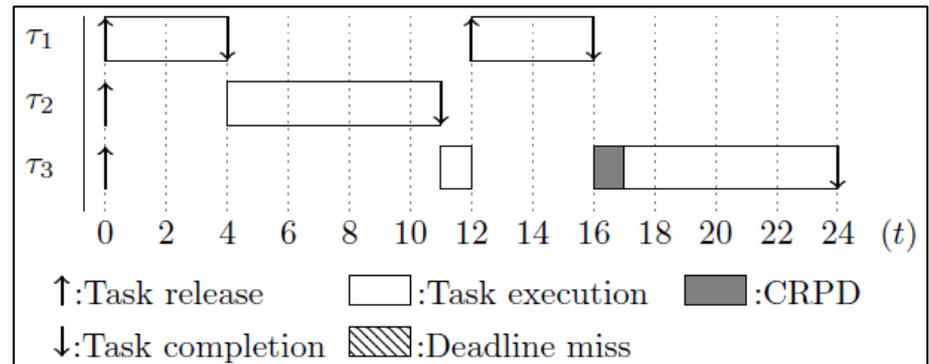
- $C'_2 = 7 (< C_2 = 8)$
- $\tau_3$  missed its deadline



- Example 1 case 2

with  $C^{on-lim}$

- Schedulable task set



# Sustainability analysis of $C^{on-lim}$

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## • Reduced capacity

**Theorem 1** : The added CRPD cannot be larger than the executed capacity of task  $\tau_i$ . In other words, if  $\tau_i$  executes in  $n - 1$  discrete intervals  $[t_a, t_a + \Delta_a)$ ,  $a \in (0, 1, \dots, n - 1)$  and experiences the preemptions costs  $\gamma_i^{t_b}$ ,  $b \in (1, \dots, n)$ , we have:

$$\sum_{b=1}^n \gamma_i^{t_b} \leq \sum_{a=0}^{n-1} \Delta_a$$

### ▪ Proof sketch: Prove by induction

- Base case:  $\gamma_i^{t_1} \leq \Delta_0$ ,  $\gamma_i^{t_1} + \gamma_i^{t_2} \leq \Delta_0 + \Delta_1$
- Inductive step: assume that

$$\sum_{b=1}^n \gamma_i^{t_b} \leq \sum_{a=0}^{n-1} \Delta_a$$

- Then we need to prove

$$\left( \sum_{b=1}^n \gamma_i^{t_b} \right) + \gamma_i^{t_{n+1}} \leq \left( \sum_{a=0}^{n-1} \Delta_a \right) + \Delta_n$$

**"CRPD added to task is limited by its executed capacity"**

# Sustainability analysis of $C^{on-lim}$

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- **Reduced capacity**

**Theorem 2 :** Assuming  $C^{on-lim}$ , a decrease of  $\Delta$  in the execution times of higher priority tasks can only lead to a maximum increase of  $\gamma$  in the execution time of a job of a lower priority task where  $\gamma \leq \Delta$

- ***"A decrease in timing requirement (by a task) achieved by a reduced capacity cannot lead to an increase of timing requirement by preemption cost"***

**Theorem 3 :** Scheduling simulation with  $C^{on-lim}$  is sustainable with regard to the capacity parameter

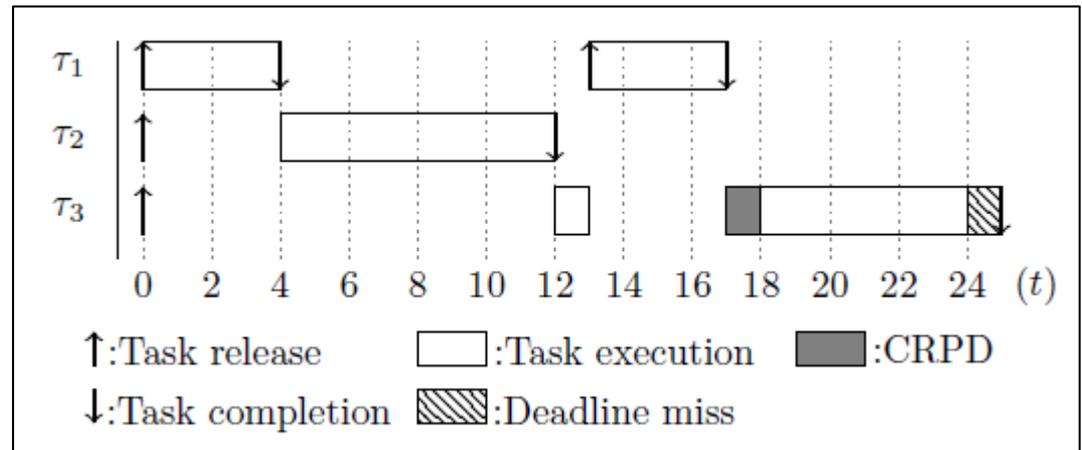
# Sustainability analysis of $C^{on-lim}$

- Larger period

**Theorem 4:** Scheduling simulation with  $C^{on-lim}$  is **not** sustainable with regard to the period parameter

- **Example 1 case 3**

- Larger period
- $T'_1 = 13 > T_1 = 12$
- $\tau_3$  missed its deadline



# Sustainability analysis of $C^{on-lim}$

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- **Larger relative deadlines**

**Theorem 5:** Scheduling simulation with  $C^{on-lim}$  is sustainable with regard to the deadline parameter

- **Fixed priority preemptive schedule is generated independently from the deadline parameter**
  - Deadlines do not influence scheduling decisions
  - We do not investigate the cases where task priorities are reassigned according to new deadlines

# Feasibility interval of $\mathcal{C}^{on-lim}$

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- **Synchronous task set**

- $F = [0, H)$ ,  $H = lcm(T_i | \forall \tau_i \in T)$ 
  - The known feasibility interval  $[0, \max(D_i))$  for synchronous task set is not applicable to systems with cache (Phavorin et al., 2017)

- **Asynchronous task set**

- $F = [0, S_n + H)$ 
  - $S_n$ : the stabilization time of the lowest priority task (Audsley, 1991)
    - Tasks are ordered by their priorities
    - $S_1 = 0_1$ ,  $S_i = \max(O_i, O_i + \left\lceil \frac{S_{i-1} - O_i}{T_i} \right\rceil \cdot T_i)$  ( $i = 2, 3, \dots, n$ )
  - This is the known feasibility interval for asynchronous task set (Audsley, 1991). Our proof was heavily inspired by the work of Audsley in 1991

# Evaluation

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- **Base configuration (Altmeyer et al., 2012)**

- **Task configuration**

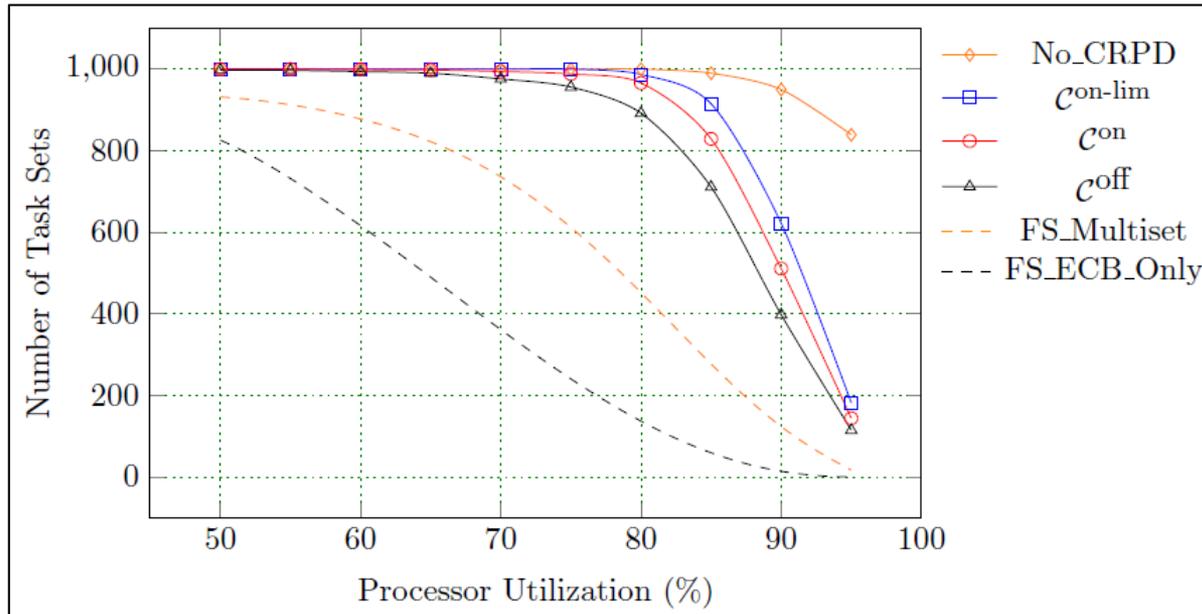
- Harmonic task sets, periods uniformly generated from 5ms to 500ms
  - Number of tasks : 10
- Processor utilization generated by the UUniFast algorithm
  - From 50% to 90% in step of 5
  - 500 task sets per utilization
  - Task capacities are generated by taking into account the generated periods and processor utilizations

- **Cache configuration**

- Direct-mapped
  - Cache size = 256
  - $BRT = 8 \mu s$
- ECB: Cache usage of each task is determined by its number of ECB
  - Generated by UUniFast algorithm for a total cache utilization of 5
- UCB: Number of ECB multiplies by a cache reuse factor
  - Cache reuse factor: 0.3

# Evaluation

- **Schedulability task set coverage**



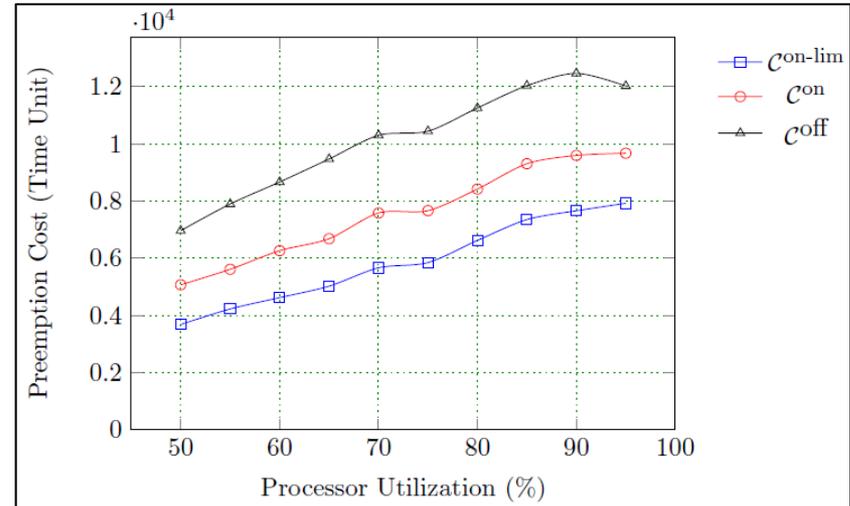
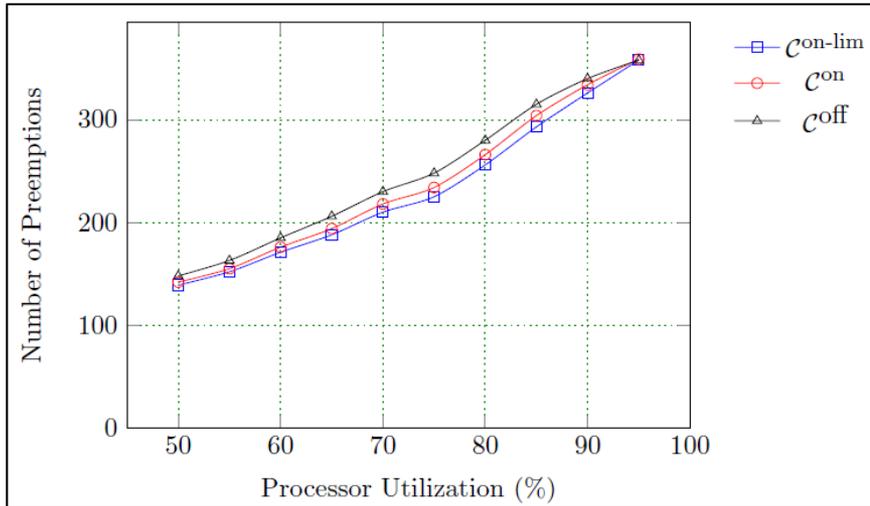
- Evaluate CRPD computation models and feasibility tests in term of schedulability task set coverage

$$sched\_coverage = \frac{\#task\_sets\_schedulable}{\#generated\_task\_sets} \%$$

- $C^{con-lim}$  have the highest coverage of 78%

# Evaluation

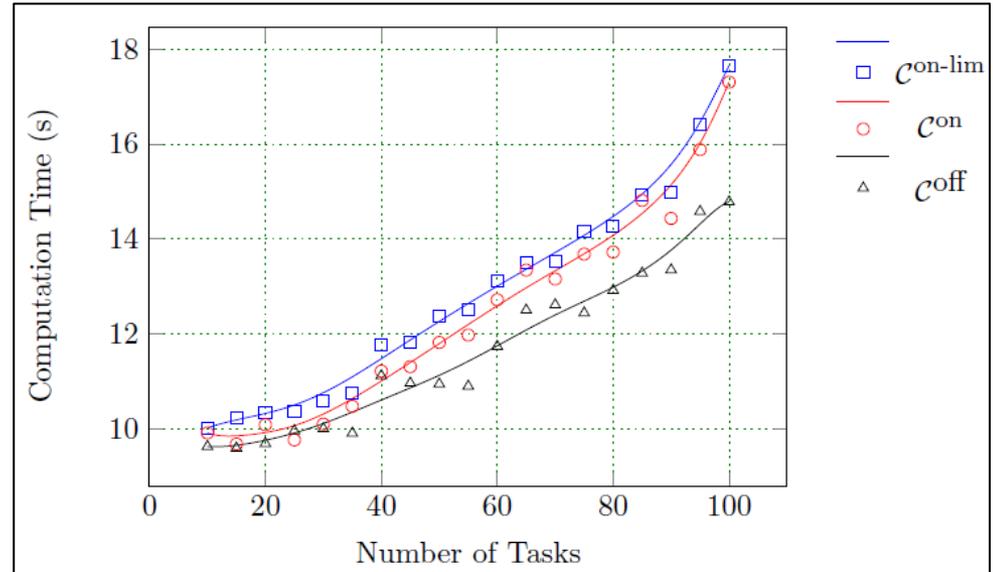
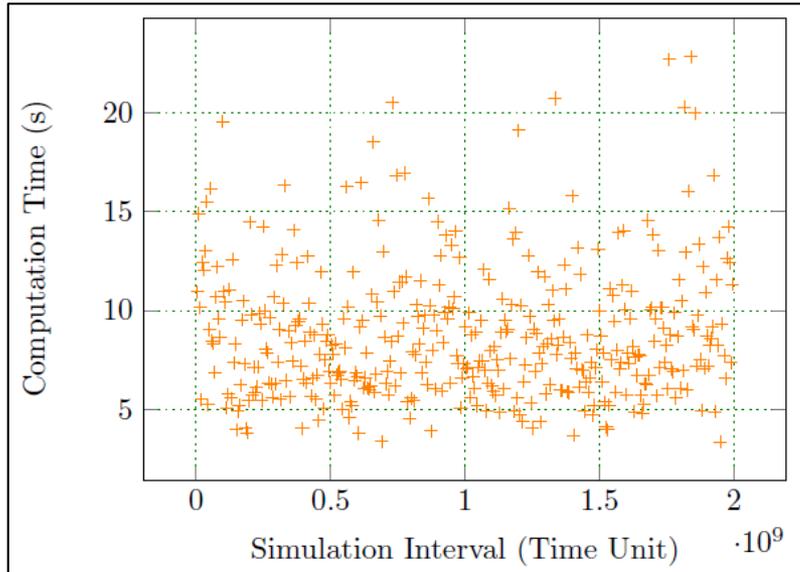
- Preemption cost and number of preemptions



- $C^{on-lim}$  number of preemptions is 7% less than  $C^{off}$  and 3% less than  $C^{on}$
- $C^{on-lim}$  preemption cost is 50% less than  $C^{off}$  and 30% less than  $C^{on}$

# Evaluation

- Performance of CRPD-aware scheduling simulator



- The CRPD computation models are implemented in the Cheddar scheduling simulator
  - Less than 25 seconds to run a simulation of  $10^9$  time units for a task set of 10
  - Less than 18 seconds to run a simulation of 100 tasks in 2.000.000 time units
  - Simulation time is largely affected by the number of tasks
- Computation time to export the complete event table is not taken into account

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- **Evaluation**

## 4. Conclusion

# Conclusion & Future work

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- **We have investigated the case of scheduling simulation with CRPD**
  - For a uniprocessor systems with many hypothesis
  - A tiny portion of the interference-aware scheduling simulation problem !
  - Implementation in Cheddar scheduling simulator
- **Problems identified**
  - What to put in our models
  - Correctness: sustainability/feasibility interval
  - Technical problems: simulator implementation, I/O performance
- **Other interference sources in Cheddar**
  - Multi-core scheduling (Projet PLATO, Plasson et al., 2022)
  - DRAM model (Kim et al, 2016)
  - Kalray memory model (Tran et al., 2018)
  - Wormhole NoC Model (Dridi et al., 2021)